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# Assessing the Numerical Accuracy of JMP® 16



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#### **Measuring Accuracy**

There are many sources of error in statistical computation, including rounding error, truncation error, and the finite-precision inaccuracy involved in representing a number in binary form.

To measure these sources of error, we looked at the significant digits reported by JMP calculations. Significant digits are the first nonzero digit and all succeeding digits. For example, 3.14159 has six significant digits, whereas 0.00314 has three. A frequently used measure of the number of correct significant digits is the (common) logarithm of the relative error (LRE). The LRE is calculated as follows:

LRE = -log(|q - c|/|c|)

where *q* is the reported value and *c* is the expected value. This quantity is not defined when q = c. In that situation, the LRE is given the value of the number of significant digits in *c*. Also, there are situations where the expected value is zero, which also results in an undefined LRE. In these cases, the LRE is defined as the logarithm of the absolute error

LRE = -log(|q|)

The LRE is approximately analogous to the number of significant digits of accuracy of a reported value compared with its expected value.

It is worth noting that the LRE is valid only for values of *q* that are close to *c*. Therefore, any calculated value that differs from *c* by more than a factor of 2 is set to zero. Finally, any value of the LRE greater than the number of digits in *c* is set to the number of digits in *c*.

We use the Greek symbol lambda ( $\lambda$ ), with a subscript, to represent the LRE. The subscript denotes the parameter to be estimated. For example,  $\lambda_{rsq}$  is the LRE between a reported r square value and its expected value.

## **Statistical Standards**

The National Institute of Standards and Technology (NIST) provides the Statistical Reference Data Sets (StRD) to assist in the evaluation of the numerical accuracy of statistical software. More information about these data sets is available at <a href="http://www.itl.nist.gov/div898/strd/">www.itl.nist.gov/div898/strd/</a>.

The StRD data sets are the subject of this paper.

The following sections report the results of tests that were run in JMP® 16 and JMP® Pro 16. All tests used the same build date: February 5, 2021. The tests were run for 64-bit systems on the following Windows versions: Windows 7 and Windows 10. The tests were run for 64-bit systems on the following macOS versions: El Capitan, Sierra, High Sierra, and Mojave.

## **Univariate Results**

The univariate tests consist of nine data sets, ranging from 3 to 5000 data points. Each data set has certified values to 15 decimal places for the mean ( $\mu$ ), standard deviation ( $\sigma$ ), and first-order autocorrelation ( $\rho$ ). Therefore, a  $\lambda$  of 15 indicates perfect agreement with NIST certified values. Results for  $\mu$  and  $\sigma$  were calculated using the JMP Distribution platform. Values of  $\rho$  came from the Time Series platform. The results are presented in Figure 1. These results are the same for all Windows and macOS operating systems that we support.

Data Set	Difficulty	$\lambda_{\mu}$	$\lambda_{\sigma}$	λρ
PiDigits	Low	15.0	14.9	13.0
Lottery	Low	15.0	15.0	15.0
Lew	Low	15.0	15.0	15.0
Mavro	Low	15.0	13.1	13.7
Michaelso	Average	15.0	13.8	13.4
NumAcc1	Average	15.0	15.0	15.0
NumAcc2	Average	14.0	14.6	13.6
NumAcc3	Average	15.0	9.4	11.2
NumAcc4	High	15.0	8.2	9.0

Table 1: Univariate Results

# **Analysis of Variance Results**

The Analysis of Variance (ANOVA) tests contain eleven data sets, with 5 to 2001 values for each level. As in the case of the previous white paper, only the LREs of F,  $R^2$ , and residual standard deviation are presented here. Again, 15 decimal places are provided in the certified values, so a score of 15 in the table corresponds to perfect agreement.

JMP provides two methods of calculating an ANOVA for two-variable cases. Its most direct method is through the Fit Y by X platform, designed specifically for bivariate data. The Fit Model platform, used for fitting general linear models, can also be used. Much of the literature on numerical accuracy reports results only for one method per software application. However, we report methods for both platforms because JMP uses distinct calculation routines for the two platforms. Results using the Fit Y by X platform are reported in Table 2, and results using the Fit Model platform are reported in Table 3. These results are the same for all Windows and macOS operating systems that we support.

Data Set	Difficulty	$\lambda_{F}$	$\lambda_{rstd}$	$\lambda_{rsq}$
SiRstv	Low	12.3	13.1	12.4
SmLs01	Low	13.9	14.4	14.2
SmLs02	Low	13.4	13.8	13.7
SmLs03	Low	12.3	12.8	12.6
AtmAgWt	Average	8.3	9.2	8.4
SmLs04	Average	8.2	8.8	8.5
SmLs05	Average	8.0	8.6	8.2
SmLs06	Average	6.1	6.8	6.4
SmLs07	High	2.4	3.0	2.7
SmLs08	High	1.9	2.5	2.1
SmLs09	High	0.3	0.8	0.5

Table 2: Analysis of Variance (ANOVA) Results Using Fit Y by X

#### Table 3: Analysis of Variance (ANOVA) Results Using Fit Model

Data Set	Difficulty	$\lambda_{\mathrm{F}}$	$\lambda_{rstd}$	$\lambda_{rsq}$
SiRstv	Low	13.0	13.4	13.1
SmLs01	Low	14.4	15.0	14.6
SmLs02	Low	13.7	14.1	14.0
SmLs03	Low	12.4	12.9	12.6
AtmAgWt	Average	10.1	11.2	10.2
SmLs04	Average	10.4	10.5	10.7
SmLs05	Average	10.2	10.5	10.4
SmLs06	Average	10.1	10.5	10.4
SmLs07	High	4.3	4.5	4.6
SmLs08	High	3.8	4.5	4.1
SmLs09	High	3.4	4.5	3.7

#### **Linear Regression Results**

The linear regression portion of the test consists of eleven data sets containing 3 to 82 data points and 1 to 11 parameters to be estimated. Each data set contains values that have been certified to 15 digits. Certified values are available for each parameter's estimate, residual standard deviation  $R^2$ , and the entire analysis of variance table (which provides the residual sum of squares).

As is the case with the ANOVA results, JMP provides two methods of fitting linear regressions: The Fit Y by X platform and the Fit Model platform. Results for each are provided for LREs of the parameter estimate  $\beta$ , its standard deviation *s*, and the residual sum of squares *rss*.

JMP also does not report an *R*<sup>2</sup> when the intercept is missing. This is the case in both the Fit Y by X and Fit Model platforms. Therefore, the two NoInt data sets have "NR" as their LRE for *R*<sup>2</sup>. Similarly, the Longley data set requires a multilinear fit, which is not available in the Fit Y by X platform. Therefore, results for Longley are listed as "NR" in the Fit Y by X tables (Table 4), but with LREs in the Fit Model tables (Table 5). Also, the Filip data requires a tenth degree polynomial fit that is not available in either the Fit Y by X or Fit Model platforms. Therefore, the results for Filip are listed as "NR" in all the following tables. These results are the same for all Windows and macOS operating systems that we support.

Data Set	Difficulty	Parameter	$\lambda_{\beta}$	$\lambda_{\rm s}$	$\lambda_{ m rss}$	$\lambda_{rsq}$
Norris	Low	β0	12.0	10.8	10.8	15.0
		β1	14.3	10.8		
Pontius	Low	β0	11.2	8.4	8.4	15.0
		β1	13.8	8.4		
		β2	12.1	8.4		
NoInt1	Average	β1	14.7	13.4	13.5	NR
NoInt2	Average	β1	15.0	14.6	14.7	NR
Filip	High	NR	NR	NR	NR	NR
Longley	High	NR	NR	NR	NR	NR
Wampler1	High	β0	8.4	15.0	15.0	15.0
		β1	8.0	15.0		
		β2	8.4	15.0		
		β3	9.2	15.0		

Table 4: Linear Regression Results Using Fit Y by X

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Data Set	Difficulty	Parameter	$\lambda_{\beta}$	$\lambda_{\rm s}$	$\lambda_{rss}$	$\lambda_{rsq}$
		β4	10.4	15.0		
		β5	12.1	15.0		
Wampler2	High	β0	12.8	15.0	15.0	15.0
		β1	11.8	15.0		
		β2	10.8	15.0		
		β3	10.5	15.0		
		β4	10.7	15.0		
		β5	11.3	15.0		
Wampler3	High	β0	8.4	11.3	11.7	15.0
		β1	8.0	10.9		
		β2	8.4	10.8		
		β3	9.2	10.8		
		β4	10.4	10.8		
		β5	12.1	10.8		
Wampler4	High	β0	8.4	11.5	14.7	15.0
		β1	8.0	10.9		
		β2	8.4	10.9		
		β3	9.2	10.8		
		β4	10.4	10.8		
		β5	12.1	10.8		
Wampler5	High	β0	8.4	11.5	14.8	13.7
		β1	8.0	10.9		
		β2	8.4	10.9		
		β3	9.2	10.8		
		β4	10.4	10.8		
		β5	12.1	10.8		

Table 4: Linear Regression Results Using Fit Y by X (Continued)

Data Set	Difficulty	Parameter	$\lambda_{eta}$	$\lambda_{\rm s}$	$\lambda_{rstd}$	$\lambda_{\text{rsq}}$
Norris	Low	β0	12.4	10.8	10.8	15.0
		β1	14.3	10.8		
Pontius	Low	β0	11.5	9.3	9.3	15.0
		β1	14.1	9.3		
		β2	12.5	9.3		
NoInt1	Average	β1	14.7	13.4	13.5	NR
NoInt2	Average	β1	15.0	14.6	14.7	NR
Filip	High	NR	NR	NR	NR	NR
Longley	High	β0	13.5	14.7	13.5	15.0
		β1	12.5	13.9		
		β2	12.9	13.6		
		β3	13.5	13.7		
		β4	14.0	13.6		
		β5	12.2	13.5		
		β6	13.5	14.6		
Wampler1	High	β0	6.7	15.0	15.0	15.0
		β1	6.3	15.0		
		β2	6.8	15.0		
		β3	7.6	15.0		
		β4	8.9	15.0		
		β5	10.6	15.0		
Wampler2	High	β0	12.1	15.0	15.0	15.0
		β1	11.0	15.0		
		β2	10.5	15.0		
		β3	10.5	15.0		
		β4	10.8	15.0		
		β5	11.6	15.0		
Wampler3	High	β0	6.7	10.7	10.8	15.0

Table 5: Linear Regression Results Using Fit Model

Data Set	Difficulty	Parameter	$\lambda_{eta}$	$\lambda_{\rm s}$	$\lambda_{rstd}$	$\lambda_{rsq}$
		β1	6.3	10.5		
		β2	6.8	10.4		
		β3	7.6	10.4		
		β4	8.9	10.4		
		β5	10.6	10.4		
Wampler4	High	βΟ	6.7	11.3	14.5	15.0
		β1	6.3	10.7		
		β2	6.8	10.6		
		β3	7.6	10.6		
		β4	8.9	10.6		
		β5	10.6	10.6		
Wampler5	High	βΟ	6.7	11.3	14.8	13.7
		β1	6.4	10.7		
		β2	6.9	10.6		
		β3	7.7	10.6		
		β4	9.0	10.6		
		β5	10.7	10.6		

Table 5: Linear Regression Results Using Fit Model (Continued)

# **Nonlinear Regression Results**

The Nonlinear regimen consists of twenty-seven data sets, with six to 250 data points and two to nine parameters. The certified values are presented to only eleven decimal places in this suite of tests, so an LRE of 11 implies perfect agreement with the standard.

- See Table 6 for Windows
- See Table 7 for macOS

Data Set	Difficulty	Parameter	$\lambda_{eta}$	$\lambda_{\beta std}$	$\lambda_{\rm sse}$	$\lambda_{rstd}$
Misra1a	Low	β1	9.6	9.3	10.4	10.6
		β2	9.6	10.6		
Chwirut2	Low	β1	7.4	7.9	11.0	10.8

 Table 6: Nonlinear Regression Results for Windows

Data Set	Difficulty	Parameter	$\lambda_{eta}$	$\lambda_{\beta std}$	$\lambda_{\rm sse}$	$\lambda_{rstd}$
		β2	7.8	8.3		
		β3	7.7	9.0		
Chwirut1	Low	β1	9.3	9.7	11.0	10.9
		β2	9.8	10.3		
		β3	9.6	11.0		
Lanczos3	Low	β1	9.2	8.3	10.5	11.0
		β2	9.5	8.3		
		β3	9.9	8.3		
		β4	10.0	8.3		
		β5	10.2	8.3		
		β6	10.7	8.3		
Gauss1	Low	β1	11.0	11.0	11.0	11.0
		β2	10.9	10.7		
		β3	11.0	11.0		
		β4	11.0	11.0		
		β5	10.6	11.0		
		β6	11.0	11.0		
		β7	10.8	11.0		
		β8	10.7	11.0		
Gauss2	Low	β1	11.0	10.7	10.6	10.6
		β2	11.0	10.8		
		β3	10.3	10.9		
		β4	10.3	10.1		
		β5	10.4	10.9		
		β6	10.7	10.5		
		β7	11.0	9.9		
		β8	10.0	9.9		
DanWood	Low	β1	10.0	10.1	11.0	11.0
		β2	10.2	10.8		

Table 6: Nonlinear Reg	gression Results :	for Windows (	(Continued)
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Data Set	Difficulty	Parameter	$\lambda_{eta}$	$\lambda_{\beta std}$	$\lambda_{\rm sse}$	$\lambda_{rstd}$
Misra1b	Low	β1	10.8	10.8	11.0	11.0
		β2	10.8	11.0		
Kirby2	Average	β1	8.5	9.3	11.0	10.7
		β2	8.6	9.0		
		β3	8.8	8.9		
		β4	8.6	8.8		
		β5	9.1	9.0		
Hahn1	Average	β1	8.4	9.1	10.5	11.0
		β2	8.5	9.0		
		β3	8.8	9.0		
		β4	8.2	9.2		
		β5	9.6	9.4		
		β6	8.9	9.0		
		β7	8.4	9.2		
Nelson	Average	β1	10.8	10.6	10.9	11.0
		β2	10.9	11.0		
		β3	11.0	10.9		
MGH17	Average	β1	9.3	10.3	11.0	11.0
		β2	7.9	7.3		
		β3	7.8	7.3		
		β4	8.4	7.7		
		β5	8.3	8.0		
Lanczos1	Average	β1	11.0	3.0	2.7	3.0
		β2	10.5	3.0		
		β3	11.0	3.0		
		β4	10.9	3.0		
		β5	10.6	3.0		
		β6	11.0	3.0		
Lanczos2	Average	β1	11.0	8.3	9.9	10.5

Table 6: Nonlinear Regression Results for Windows (Continued)

Data Set	Difficulty	Parameter	$\lambda_{eta}$	$\lambda_{\beta std}$	$\lambda_{\rm sse}$	$\lambda_{rstd}$
		β2	10.3	8.4		
		β3	11.0	8.3		
		β4	11.0	8.3		
		β5	10.7	8.3		
		β6	11.0	8.3		
Gauss3	Average	β1	11.0	11.0	10.9	10.7
		β2	10.9	10.4		
		β3	10.6	10.4		
		β4	10.5	11.0		
		β5	11.0	11.0		
		β6	11.0	10.6		
		β7	10.4	10.9		
		β8	10.6	11.0		
Misra1c	Average	β1	11.0	11.0	11.0	11.0
		β2	10.8	10.6		
Misra1d	Average	β1	11.0	10.8	11.0	11.0
		β2	11.0	11.0		
Roszman1	Average	β1	11.0	11.0	11.0	11.0
		β2	10.4	10.9		
		β3	10.8	11.0		
		β4	10.9	10.7		
Enso	Average	β1	9.9	9.7	11.0	11.0
		β2	9.4	10.6		
		β3	8.7	10.3		
		β4	8.8	8.2		
		β5	8.2	8.0		
		β6	7.4	8.6		
		β7	8.5	8.0		
		β8	6.4	8.8		

Table 6: Nonlinear Regression Results for Windows (Continued)

Data Set	Difficulty	Parameter	$\lambda_{eta}$	$\lambda_{\beta std}$	$\lambda_{\rm sse}$	$\lambda_{rstd}$
		β9	8.1	7.6		
Mgh09	High	β1	8.7	8.0	11.0	11.0
		β2	7.4	7.5		
		β3	7.9	7.6		
		β4	7.5	7.6		
Thurber	High	β1	10.2	9.0	11.0	10.6
		β2	8.4	7.0		
		β3	8.1	7.0		
		β4	8.0	7.0		
		β5	8.4	7.0		
		β6	8.3	7.0		
		β7	7.6	7.0		
BoxBOD	High	β1	9.8	9.4	10.4	11.0
		β2	9.2	9.2		
Rat42	High	β1	9.6	8.9	11.0	10.4
		β2	9.8	9.3		
		β3	9.3	9.4		
Mgh10	High	β1	11.0	9.7	11.0	11.0
		β2	11.0	9.8		
		β3	10.8	9.8		
Eckerle4	High	β1	10.0	9.8	10.7	11.0
		β2	9.6	9.6		
		β3	10.9	9.6		
Rat43	High	β1	9.6	8.7	11.0	11.0
		β2	8.4	8.6		
		β3	8.5	8.4		
		β4	8.4	8.6		
Bennett5	High	β1	7.3	6.6	11.0	10.6
		β2	8.0	6.6		

 Table 6: Nonlinear Regression Results for Windows (Continued)

Data Set	Difficulty	Parameter	$\lambda_{eta}$	$\lambda_{\beta std}$	$\lambda_{\rm sse}$	$\lambda_{rstd}$
		β3	8.0	6.6		

Table 6: Nonlinear	Regression	<b>Results</b> for	Windows	(Continued)
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Table 7: Nonlinear Regression Results for macOS

Data Set	Difficulty	Parameter	$\lambda_{\beta}$	$\lambda_{\beta std}$	$\lambda_{\rm sse}$	$\lambda_{rstd}$
Misra1a	Low	β1	8.3	7.9	10.4	10.6
		β2	8.2	9.4		
Chwirut2	Low	β1	7.7	8.1	11.0	10.8
		β2	8.0	8.6		
		β3	8.0	9.3		
Chwirut1	Low	β1	10.5	10.7	11.0	10.9
		β2	11.0	10.8		
		β3	11.0	11.0		
Lanczos3	Low	β1	9.3	8.7	10.5	11.0
		β2	9.6	8.8		
		β3	10.0	8.6		
		β4	10.1	8.6		
		β5	10.3	8.6		
		β6	10.8	8.6		
Gauss1	Low	β1	11.0	9.6	11.0	11.0
		β2	8.9	8.7		
		β3	11.0	9.8		
		β4	11.0	11.0		
		β5	10.6	9.8		
		β6	11.0	10.6		
		β7	10.8	10.9		
		β8	10.8	10.3		
Gauss2	Low	β1	11.0	10.7	10.6	10.6
		β2	11.0	10.8		

Data Set	Difficulty	Parameter	$\lambda_{\beta}$	$\lambda_{\beta std}$	$\lambda_{\rm sse}$	$\lambda_{rstd}$
		β3	10.3	10.9		
		β4	10.3	10.1		
		β5	10.4	10.9		
		β6	10.7	10.5		
		β7	11.0	9.9		
		β8	10.0	9.9		
DanWood	Low	β1	10.0	10.1	11.0	11.0
		β2	10.2	10.8		
Misra1b	Low	β1	10.9	10.8	11.0	11.0
		β2	10.9	11.0		
Kirby2	Average	β1	8.5	9.3	11.0	10.7
		β2	8.6	9.0		
		β3	8.8	8.9		
		β4	8.6	8.8		
		β5	9.1	9.0		
Hahn1	Average	β1	8.4	9.1	10.5	11.0
		β2	8.5	9.0		
		β3	8.8	9.0		
		β4	8.2	9.2		
		β5	9.6	9.4		
		β6	8.9	9.0		
		β7	8.4	9.2		
Nelson	Average	β1	10.8	10.6	10.9	11.0
		β2	10.9	11.0		
		β3	11.0	10.9		
MGH17	Average	β1	11.0	10.8	11.0	11.0
		β2	10.7	10.3		
		β3	10.6	10.5		
		β4	11.0	10.9		

Table 7: Nonlinear Regression Results for macOS (Continued)

Data Set	Difficulty	Parameter	$\lambda_{eta}$	$\lambda_{\beta std}$	$\lambda_{\rm sse}$	$\lambda_{rstd}$
		β5	10.7	10.6		
Lanczos1	Average	β1	11.0	3.1	2.7	3.1
		β2	10.5	3.1		
		β3	11.0	3.1		
		β4	10.9	3.1		
		β5	10.6	3.1		
		β6	11.0	3.1		
Lanczos2	Average	β1	11.0	8.3	10.0	10.6
		β2	10.3	8.3		
		β3	11.0	8.3		
		β4	11.0	8.3		
		β5	10.7	8.3		
		β6	11.0	8.3		
Gauss3	Average	β1	11.0	11.0	10.9	10.7
		β2	10.9	10.4		
		β3	10.6	10.4		
		β4	10.5	11.0		
		β5	11.0	11.0		
		β6	11.0	11.0		
		β7	10.4	11.0		
		β8	11.0	11.0		
Misra1c	Average	β1	11.0	11.0	11.0	11.0
		β2	10.8	10.6		
Misra1d	Average	β1	11.0	10.8	11.0	11.0
		β2	11.0	11.0		
Roszman1	Average	β1	11.0	11.0	11.0	11.0
		β2	11.0	11.0		
		β3	10.8	11.0		
		β4	11.0	10.9		

Table 7: Nonlinear Regression Results for macOS (Continued)

Data Set	Difficulty	Parameter	$\lambda_{eta}$	$\lambda_{\beta std}$	$\lambda_{\rm sse}$	$\lambda_{rstd}$
Enso	Average	β1	10.6	10.0	11.0	11.0
		β2	9.8	11.0		
		β3	9.0	10.6		
		β4	9.1	8.5		
		β5	8.6	8.3		
		β6	7.7	8.9		
		β7	8.8	8.3		
		β8	6.8	9.1		
		β9	8.5	7.9		
Mgh09	High	β1	8.7	8.0	11.0	11.0
		β2	7.4	7.5		
		β3	7.9	7.6		
		β4	7.5	7.6		
Thurber	High	β1	10.2	8.9	11.0	10.6
		β2	8.3	6.9		
		β3	8.0	6.9		
		β4	7.9	6.9		
		β5	8.3	6.9		
		β6	8.2	6.9		
		β7	7.5	6.9		
BoxBOD	High	β1	9.8	9.4	10.4	11.0
		β2	9.2	9.2		
Rat42	High	β1	9.6	8.9	11.0	10.4
		β2	9.8	9.3		
		β3	9.3	9.4		
Mgh10	High	β1	11.0	9.7	11.0	11.0
		β2	11.0	9.8		
		β3	10.8	9.8		
Eckerle4	High	β1	10.0	9.8	10.7	11.0

Table 7: Nonlinear Regression Results for macOS (Continued)

Data Set	Difficulty	Parameter	$\lambda_{eta}$	$\lambda_{\beta std}$	$\lambda_{\rm sse}$	$\lambda_{rstd}$
		β2	9.6	9.6		
		β3	10.9	9.6		
Rat43	High	β1	10.2	9.3	11.0	11.0
		β2	9.0	9.2		
		β3	9.2	9.0		
		β4	9.0	9.2		
Bennett5	High	β1	7.3	6.3	11.0	10.6
		β2	8.0	6.3		
		β3	8.0	6.3		

Table 7: Nonlinear Regression Results for macOS (Continued)

## **Appendix 1 Replicating JMP 16 Numerical Accuracy Results**

To reproduce the results reported in these tables:

- 1. Download the compressed archive of the NIST testing framework (available at <a href="http://www.jmp.com/qualitystatement/">www.jmp.com/qualitystatement/</a>).
- 2. Uncompress the archive to a directory of your choice.
- 3. Locate and execute the RunNISTTests.jsl script. The script creates the window shown in Figure 1. This window enables you to execute either all tests or selected tests. See Figure 2 for an example of the report that is generated when the tests are run.

The NIST testing framework can facilitate operational qualification or validation of JMP. The testing framework displays the LRE and the certified minimum LRE for each reported value. The testing framework also displays the relative error threshold (RET) value; the RET value is calculated based on the certified minimum LRE. The RET represents the minimum computational accuracy that we deem acceptable for our software.

If the LRE is greater than or equal to the certified minimum LRE, the test is passed. The resulting report shows the status of the test, the NIST standard value, the value actually computed, the LRE, the certified minimum LRE, and the RET. (The RET appears in a hidden column.) In this way, the tests serve as a tool to demonstrate that JMP is operating as expected.

**Note:** This framework is a specialized version of the framework described in the article titled "Unit Tests: Automated JSL Testing" that appeared in the Fall 2007 (issue #23) edition of the *JMPer Cable*<sup>®</sup> newsletter. The framework consists of a set of JSL scripts and

JMP data tables corresponding to each of the StRD data sets mentioned in the previous sections. See Appendix 2 for additional details.

Figure 1: NIST Test Driver

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## Figure 2: NIST Test Report

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## **Appendix 2 NIST Testing Framework**

The NIST framework consists of a set of JSL scripts and JMP data tables. It is intended to be host independent and should work for any version of JMP beginning with version 7. The architecture is as follows:

#### Figure 3: NIST Testing Framework



The GUI driver script (RunNISTTests.jsl) can reside anywhere in your file system. The NIST test scripts and associated data tables must reside in a subdirectory, named tests/NIST/, of the directory where the driver script is located. In addition, to be recognized by the driver, test scripts use a prefix of test (for example, testMavro.jsl).

NIST tests are specified as JSL scripts that access test data from JMP data tables. Individual test cases (for example, parameter estimates) are specified by way of a function named ut assert LRE() that is defined by the GUI driver. The prototype of the function is

```
ut assert LRE( expression, expected value, minimum LRE )
```

where the expression argument specifies the actual result and the expected value argument the expected result. A test case is considered a success (or a pass) if the computed LRE is greater than or equal to the value specified by the minimum LRE argument. Test cases also pass if the expected and actual values are both missing.

Note that the framework is a JSL application and the scripts that constitute the framework are provided in unencrypted form. Users can therefore change the driver script, associated utility scripts, or the test scripts, if necessary. Users can also add additional test scripts to the framework. As long as a few simple conventions (described in the following section) are followed, the driver automatically detects these scripts and makes them available for execution.

#### **Adding Test Scripts to the Framework**

- 1. Use the pattern below as a guide when writing your script.
- 2. Ensure that the script is stored in the tests/NIST/subdirectory.
- 3. Ensure that the script name has the test prefix (for example, testMavro.jsl).

#### **NIST Test Script Pattern**

```
Names Default to Here( 1 ); // Open data table
```

```
dt = Open( < name > );
// Expected results and certified LRE values
expected = < expected value >;
certLRE = < certified minimum LRE value >;
// Launch platform and define a reference to the report
obj = < platform launch expression >;
rpt = obj << report;
// Navigate display tree and get actual results
actual = rpt[ < subscript > ] << get as matrix;
// Invoke ut assert LRE function to execute numerical accuracy tests
ut assert LRE( expr(actual), expected, certLRE );
close(dt, no save);
wait(0); // give window a chance to close
```

## References

Creighton, L. and Ding, J. (2000). "Assessing the numerical accuracy of JMP". *SAS Whitepaper*.

McCullogh, B. D. (1998). "Assessing the reliability of statistical software: Part I". *The American Statistician*, v52, n4 (November 1998), 358-366.

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